Limits to biodiversity cycles from a unified model of mass-extinction events

Georg Feulner

Earth System Analysis, Potsdam Institute for Climate Impact Research
P.O. Box 60 12 03, D–14412 Potsdam, Germany
e-mail: feulner@pik-potsdam.de

Abstract

Episodes of species mass extinction dramatically affected the evolution of life
on Earth, but their causes remain a source for debate. Even more controversy
surrounds the hypothesis of periodicity in the fossil record, with conflicting
views still being published in the scientific literature, often even based on the
same state-of-the-art data-sets. From an empirical point of view, limitations
of the currently available data on extinctions and possible causes remain an
important issue. From a theoretical point of view, it is likely that a focus on
single extinction causes and strong periodic forcings has strongly contributed
to this controversy. Here I show that if there is a periodic extinction signal
at all, it is much more likely to result from a combination of a comparatively
weak periodic cause and various random factors. Tests of this unified model of
mass extinctions on the available data show that the model is formally better
than a model with random extinction causes only. However, the contribution
of the periodic component is small compared to factors such as impacts or
volcanic eruptions.

Keywords: *evolution, macroevolution, mass extinctions, paleobiology*

1   Mass extinctions in the history of life

During the Phanerozoic (the last 542 million years in Earth's history), the fossil record shows ample evidence for major biological extinction events (Bambach, 2006). Although the precise number of mass extinctions is a matter of definition and depends on the analysed data-set (Bambach, 2006, Alroy, 2008), a few mass extinction events stand out due to their particularly dramatic loss of diversity (Raup & Sepkoski, 1982, Alroy, 2008), including the famous end-Permian and end-Cretaceous extinctions 251 and 65 million years ago.

No consensus has been reached yet concerning the ultimate causes and kill mechanisms of these biological crises. Among the usual suspects are large-scale volcanic eruptions and associated short-term aerosol cooling and long-term warming (Wignall, 2005), meteorite impacts responsible for nuclear winter-like conditions (Toon *et al.*, 1997), sea-level changes impacting on the marine biosphere (Hallam & Wignall, 1999, Peters, 2008), ocean anoxia (Wignall & Twitchett, 1996), and the adverse effects of abrupt climatic changes resulting from various climate forcings (Crowley & North, 1988). Of course, combinations of different factors might be responsible for mass extinctions (Arens & West, 2008). Furthermore, one might not be looking at a biological signal but a sampling signal, e.g. due to changes in sea level influencing the amount of marine sedimentary rock (Smith & McGowan, 2005).

The confusion is further amplified by repeated suggestions for regular cycles in extinction rates or species diversity of marine invertebrates (fluctuations in diversity can be caused by changes in species origination, extinction or both). Earlier studies suggested a 26-million-years periodicity in extinction (Raup & Sepkoski, 1984), which was the basis for the hypothesis of an unknown object orbiting the Sun (Davis *et al.*, 1984, Whitmire & Jackson, 1984). The spectral signal on which this 'Nemesis' hypothesis was based was later considered spurious. However, Melott & Bambach (2010) confirmed the signal in two improved data-sets of fossil diversity, but rule out the Nemesis hypothesis due to the extremely regular timing.

More recently, evidence for a 62-million-years cycle in marine diversity was reported (Rohde & Muller, 2005). On the one hand, this result has been challenged on a number of grounds, mostly involving the statistical method (Omerbashich, 2006) and the data-set used in the analysis (Alroy, 2008). On the other hand, it has recently passed a number of critical tests using better-suited methodology (Cornette, 2007, Lieberman & Melott, 2007), a re-

analysis (Melott, 2008) using the Paleobiology Database (Alroy, 2008) and thus an improved data-set of fossil diversity, and a comprehensive analysis of three different and independent marine diversity data-sets (Melott & Bambach, 2011).

Hence cycles in fossil diversity or extinction remain a highly controversial topic, yet the disagreement between different studies is intriguing, especially since the analysis is often based on the same data. If the case for biodiversity cycles thus appears far from settled from the analysis of the fossil record, it is even less so concerning potential causes.

A number of causes and mechanisms for periodic diversity fluctuations have been suggested in the literature, mostly focusing on causes for extinction rather than origination (Rohde & Muller, 2005, Bailer-Jones, 2009). Sea-level changes and episodes of large volcanic eruptions are the most widely accepted terrestrial causes of major extinctions, and the question has been investigated whether these could operate periodically. Periodic changes of sea level would either require periodic changes in climate (thus requiring an unknown source for regular changes in climate forcing) or periodic uplift of continents (Hallam, 1984). As for volcanic eruptions, large igneous provinces (caused by large magma flows emerging over short periods of time) indeed show some evidence for weak cycles with periods of ~ 15, ~ 30 and ~ 60 million years over the last 300 million years (Prokoph *et al.*, 2004). Such periodic volcanism could be either caused by periodic mantle plumes (Schaeffer & Manga, 2001) or, more speculatively, by periodic impacts of minor bodies from space (see below).

Astronomical phenomena are a source of periodicity in a wide range of frequencies, thus many authors have argued for an astronomical origin of the periodicity in the fossil record. Periodic enhancement of the impact rate of comets could be triggered by perturbations of the Oort cloud due to periodic passages of Giant Molecular Clouds or capture of minor bodies during the Sun's orbit around the Galactic centre. These could happen either when the Sun crosses the Galactic mid-plane (Rampino & Stothers, 1984) or the Milky Way's spiral arms (Napier & Clube, 1979). Furthermore, the Oort cloud might be perturbed by Galactic tidal forces (Heisler *et al.*, 1987). The connection between long-period comets from the Oort cloud and mass extinctions has been criticised, however (Kaib & Quinn, 2009). Furthermore, recent models for the Galactic structure show an asymmetric structure and exclude strictly periodic spiral-arm crossings with periods below ~ 500 million years (Overholt *et al.*, 2009). Finally, Galactic mid-plane crossings occur

every about 30 million years, a period which does not match the 62 million-year cycle, although it is close to the more ambiguous shorter period in fossil diversity (Raup & Sepkoski, 1984, Melott & Bambach, 2010).

Supernova explosions have been suggested as causes of mass extinctions (Ellis & Schramm, 1995), and their rate could be periodically enhanced during passages through the Milky Way's plane or spiral arms, although the periods, again, do not match, and the density of supernova may only be slightly enhanced in these higher-density regions (Bailer-Jones, 2009).

Finally, Galactic cosmic rays have been suggested as cause of periodic mass extinctions, most convincingly for the 62-million-year period in the fossil record (Medvedev & Melott, 2007). In this scenario, the Earth becomes exposed to enhanced rates of cosmic rays from the Virgo cluster of galaxies whenever it is far North of the Galactic plane. Both changes in climate and biologically harmful radiation have been invoked as extinction mechanisms, although both effects are likely very small.

Traditionally, many investigations of the causes of mass extinctions and of possible periodic extinctions have focused on single causes and (so far unsuccessful) searches for strong periodic forcings of biodiversity. It can be argued that – apart from limitations of the available data – this is the primary reason for the longstanding controversy about periodic extinctions in the fossil record. In reality one could very well be looking at a combination of different extinction causes, including random events and one or more periodic driver(s). This can be viewed as an extension of the 'press-pulse model' for extinctions indipendently proposed by Arens & West (2008), in which a press disturbance puts stress on the ecosystems and acts together with a sudden and catastrophic pulse disturbance to produce the major extinction events observable in the fossil record.

Even if a periodic contribution to the Earth's extinction record exists, however, the questions arise why its signature is so difficult to detect, how important the periodic component is in comparison to other factors, and what limits can be placed to it. This will be the focus of this paper.

This paper is organised as follows. Section 2 looks at the causes of extinction events on a rather fundamental level and explores different options. In Section 3 I introduce a conceptual model for mass extinctions combining periodic and random extinction causes. A special case of this model with a weak periodic disturbance of the biosphere is discussed in Section 4, and Section 5 presents a first test of this hypothesis using the best available data.

Finally, Section 6 concludes with a discussion and summary of the results.

2   Weighing the options

The discussions above clearly demonstrate that the scientific community has not yet reached a consensus on two important questions concerning the origin of major extinctions: (1) Are the extinction peaks observed in the fossil record triggered by one single cause or multiple causes? (2) Are there any periodic causes for a decrease in diversity? Finding an answer to these fundamental questions appears to be a pre-requisite for solving the problem of the causes of extinction events in the history of life on Earth.

From studies of the origins of extinctions one can conclude that there were many catastrophic events such as massive volcanic eruptions or bolide impacts in Earth's history for which a major impact on the biosphere is likely (e.g. Wignall, 2004). This would imply that mass extinction events could be caused by a variety of triggers, although this would have to be demonstrated beyond doubt by detailed modelling of the causes' effects on the climate and the biosphere.

If mass extinctions are caused by several factors, and if there are periodic drivers of species extinction, one can immediately draw some conclusions about extinction causes. Either one seems to be left with the far-reaching conclusion that the various drivers of mass extinction events are in reality causally connected (e.g. by periodic impacts from space triggering the volcanic eruptions responsible for large igneous provinces), which does not seem particularly likely for a number of reasons (see, e.g., White & Saunders, 2005). Or mass extinctions would be caused by a combination of periodic and random disturbances, and in many ways this appears to be the most interesting and most likely case. This possibility will be explored making use of a conceptual model of the major extinctions in the past.

3   A unified model for mass extinctions

It will prove useful useful to think about extinction events within the framework of a simple conceptual model, which is illustrated in Figure 1. The model has two key elements, the combination of various extinction causes

acting together to produce the observed biodiversity history, and the existence of a threshold beyond which a mass-extinction event is detected or defined.

In this model, the total extinction rate as a function of time is considered as a combination of a noisy background component, a periodic component[1] and occasional random events with higher extinction rate which could be resulting from impacts from space, large-scale volcanism and the like.[2]

Furthermore, one can imagine a particular threshold extinction rate above which a particular extinction event would be detected in the fossil record or defined as true mass-extinction event.[3] It is important to note that a mass-extinction threshold defined in this way needs not necessarily be constant in time. Furthermore, while the definition of a threshold disturbance for mass extinctions seems to be well justified, the model could be extended to describe a more continuous transition between losses of biodiversity of various magnitudes.

Although it certainly is only a simplistic representation of the much more complex ecological reality, this model helps to focus on different possibilities for the origins of the major losses of biodiversity in the history of life.

4   Periodic enhancements of extinction rate

One could imagine, for example, that a periodic forcing regularly impacts on the biosphere severely enough for a massive extinction to occur, with particularly catastrophic extinction events occurring whenever a large random pulse coincides with a peak in periodic extinction forcing (see Figure 1).

There is another possibility, however, which has been often neglected so far

---

[1]In principle, there could be several periodic drivers with different amplitude, period, and phase, of course.

[2]One assumption of the model in this form is that the causes of extinctions are physical and independent of diversity itself. There is, however, evidence for density-dependent extinction rates in the data (Alroy, 2008). Since the most widely discussed drivers of major extinctions rely on physical mechanisms, and since a density-dependent component could, in principle, be added to the model, this does not affect the main conclusions of this paper.

[3]Alternatively, a threshold for mass-extinction events might exist which results from the non-linear nature of ecological networks, where small changes may trigger catastrophic changes (Holling, 1973, May, 1977, Scheffer *et al.*, 2001, van Nes & Scheffer, 2004).

in discussions of possible periodic impacts on the biosphere. In this case, which is illustrated in Figure 2, the periodic disturbance alone is not capable of causing a true mass extinction. Major extinctions are then triggered when frequent random pulses from one or more different causes are pushing the biosphere beyond the threshold during the phases of higher extinction rate caused by the weak periodic signal.[4] In this sense, the model can be viewed as an extension of the press-pulse model developed by Arens & West (2008) in which the press disturbance is periodic in nature.

The weakness of the periodic signal together with the distortions from random extinction pulses may present one reason for the controversy about potential periodicity in the fossil record.

Two conditions must be met in order to make this scenario plausible. First, the random pulses must be frequent and intense enough to cause extinction (almost) every time the periodic disturbance peaks. In mathematical terms, the average "frequency" $\langle f_{\mathrm{r}} \rangle$ – defined by the average time interval $\langle \Delta T_{\mathrm{r}} \rangle$ between random impacts, $\langle f_{\mathrm{r}} \rangle \equiv 1/\langle \Delta T_{\mathrm{r}} \rangle$ – of random pulses with extinction rate E_{r} beyond $E_{\mathrm{t}} - E_{\mathrm{b}} - 2E_{\mathrm{p}}$ (see Figure 1 for definitions) must be larger than the frequency f_{p} of the periodic signal, or

$$\langle f_{\mathrm{r}} \rangle_{E_{\mathrm{r}} > E_{\mathrm{t}} - E_{\mathrm{b}} - 2E_{\mathrm{p}}} > f_{\mathrm{p}}, \tag{1}$$

since the extinction rate E_{r} of the random pulses must be larger than the difference between the threshold E_{t} for a mass-extinction event and the sum of background extinction rate E_{b} and peak extinction rate E_{p} of the periodic driver, or $E_{\mathrm{r}} > E_{\mathrm{t}} - E_{\mathrm{b}} - 2E_{\mathrm{p}}$ to be able to push the extinction rate beyond the threshold whenever the periodic cause peaks.

Secondly, strong random impacts should not occur so often as to raise the extinction rate above the threshold even in minima of the periodic forcing, or

$$\langle f_{\mathrm{r}} \rangle_{E_{\mathrm{r}} > E_{\mathrm{t}} - E_{\mathrm{b}}} \ll f_{\mathrm{p}}. \tag{2}$$

Note that an intensity distribution following these conditions, i.e. with higher

---

[4]If the threshold is interpreted as climatic or ecological stability threshold, this is analogous to the phenomenon of stochastic resonance (Benzi *et al.*, 1982) in non-linear systems such as the Earth's climate system (e.g. Ganopolski & Rahmstorf, 2002).

intensity events being less frequent than lower intensity events, is to be expected from the distribution function of many physical quantities.

Without knowledge of E_p and E_t, it is rather difficult to assess whether the various random pulses of extinction disturbances were frequent and intense enough to satisfy these criteria. If, on the other hand, the peak amplitude E_p for a periodic forcing under investigation and an extinction threshold E_t can be quantified, one can – at least in principle – test whether these conditions are fulfilled or not.

Some conclusions concerning these two criteria, however, can be drawn from the frequency of the two most widely discussed extinction triggers, bolide impacts and flood-basalt eruptions, however. Asteroid or comet impacts of objects with diameters beyond a few kilometres are expected to affect the climate and the biosphere on global scales (Toon *et al.*, 1997) and occur every few million years or so, while larger impacts similar to the Chicxulub event occur in intervals of 100 million years or less (Chapman, 2004). About a dozen (continental) flood-basalt provinces with ages up to 300 million years are known today, corresponding to an average time interval between eruptions of about 25 million years (White & Saunders, 2005).

Assuming that the larger impacts and the flood-basalt eruptions have the potential to affect global biodiversity, these rates appear indeed high enough to trigger extinctions in connection with a hypothetical underlying periodic disturbance with the period of 62 million years as suggested in Rohde & Muller (2005). Indeed, White & Saunders (2005) and Arens & West (2008) demonstrate that major impacts and eruptions occur so frequently that impacts and eruptions coinciding in time may explain the most dramatic extinction events. Additional triggers intrinsic to the Earth system may further contribute to the frequency of random impacts on the biosphere.

The intriguing fact that not all flood-basalt eruptions and astronomical impacts have left their trace in the record of biological diversity does not invalidate this argument. This could be evidence of a further prerequisite needed for a major extinction event, which may be identical with a possible periodic extinction driver.

Beyond these qualitative arguments, the performance of the model will be tested in a more quantitative way in the following Section.

5   Confronting the model with the data

Although a conclusive test of the model described above appears to be difficult given the sparse data available today and the incomplete understanding of mass extinction mechanisms, a first assessment can be performed using information on the variation of extinction rate of marine invertebrates from the Paleobiology Database (Alroy, 2008), large igneous provinces (Ernst & Buchan 2001) and bolide impacts from the Earth Impact Database through geological time. Details on the data-sets can be found in Appendix A.

The extinction curve of marine invertebrates is approximated by a simple linear model for the (de-trended) extinction rate E as a function of age τ by minimising χ^2 (see Appendix B for details):

$$E\left(\tau\right) \;=\; a_{\mathrm{b}} + a_{\mathrm{p}}\left[\,1\,+\,\sin\left(\frac{2\pi}{T}+\varphi\right)\right] + a_{\mathrm{v}}\,V(\tau) + a_{\mathrm{i}}\,I(\tau), \qquad (3)$$

with the background extinction rate a_{b}, the amplitude a_{p}, period T and phase φ of a periodic perturbation, and coefficients a_{v} and a_{i} translating the area of large igneous provinces and the energy of bolide impacts into extinction rate.

Given the limited understanding of extinction mechanisms and the available data, this simple parametrisation of the extinction effects of volcanoes and impacts is a reasonable approximation. Note, however, that there are several problems with this approach: First, the record of large igneous provinces and impact craters is incomplete and suffers from dating problems, especially for ages beyond 250 Ma. Secondly, while a linear relation between perturbation and extinction rate is assumed, a non-linear scaling is much more likely. Thirdly, while magma area and crater diameter are certainly reasonable proxies for their environmental effects, geographic and geologic factors almost certainly influence the extinction rate as well. Fourthly, dating uncertainties cause temporal misalignment between the data. The main effect of these limitations will be rather poorly determined values for a_{v} and a_{i}.

A χ^2 approximation of the model described in Equation (3) to the observed de-trended per-taxon extinction rate of marine invertebrates is shown in Figure 3, and the best-fit parameters are given in Table 1.

Despite the fact that the overall model fit certainly is not perfect (as to be expected from the limitations outlined above), it indeed shows a weak periodic

perturbation below the threshold for true mass extinctions. Furthermore, it has been verified that the amplitude of this periodic signal is quite robust with respect to variations in the timing and scaling of the random impacts. Moreover, qualitatively similar results are obtained with a test using the older Sepkoski data-set (Rohde & Muller, 2005, Bambach, 2006) which has higher time resolution, but is not corrected for sampling bias. Finally, a fit without the periodic component yields a slightly worse approximation of the data (see Table 1). Using Akaike's Information Criterion (AIC, Burnham & Anderson 2002) to compare the models yields an AIC difference $\Delta AIC = 10.78$ and favours the model including the periodic perturbation with a weight $w = 0.9955$ over the purely random model with $w = 0.0045$.

This simple test therefore shows that the model of a weak periodic perturbation plus random impacts on the biosphere presented above is in agreement with the available data, although a more comprehensive test would require more complete data on impacts and volcanic eruptions as well as a better understanding of the scaling of biodiversity loss for these perturbations. It also demonstrates that any contribution of a periodic component to the extinction rate is small compared to random events such as impacts and volcanic eruptions.

6   Discussion

The last years have seen considerable improvement in thinking about mass-extinction events in the sense of a development from a focus on one particular event or on one particular ultimate cause towards a more complete picture. One example is the study by Arens & West (2008) who test the hypothesis that large-scale volcanism combined with impacts from space constitutes a general mechanism for mass extinctions. This is part of their more general 'press-pulse' theory in which a press disturbance puts stress on the ecosystems and acts together with sudden pulse disturbances to cause the major extinction events.

Following this pursuit of a more general theory for extinction events, a simple conceptual model for the relation between the causes and impacts of mass extinctions is presented in this paper. On the most fundamental level, two pressing questions about mass-extinction events in Earth's history require an answer and should direct future research on this issue: (1) Are major extinctions caused by one single cause or by several? (2) Are there any

periodic drivers for species extinction?

As for the first question, it appears likely that there is more than one cause for major extinctions. Indeed, the random concurrence of two impacts on the biosphere from different sources (e.g. massive volcanism and an impact from space) might be required to cause the most massive extinction events (White & Saunders, 2005, Arens & West, 2008). Answering this question requires not only a detailed understanding of the ultimate extinction causes itself, but more importantly of their effect on the biosphere. Since in most cases the link between cause and ecological impact is conveyed by the Earth's climate, paleoclimate data and climate modelling of extinction events are clearly very important (Feulner, 2009). Ultimately, of course, one would like to model the impacts on the Earth's ecosystems as well (e.g. Melott & Thomas, 2009, Martin *et al.*, 2010, for the impact of Gamma Ray Bursts on the biosphere).

The second question concerning cycles in fossil diversity remains unanswered as well. Considering the well-known deficiencies of the fossil record (e.g. Peters & Foote, 2002), sampling issues of paleobiological databases, and the difficulties of statistically sound analyses of time-series data (e.g. Bailer-Jones, 2009), it is understandable that many scientists remain skeptical about periodicity of biodiversity on time-scales of tens of millions of years. Even vastly improved data-sets such as the Paleobiology Database (Alroy *et al.*, 2008) appear to be unable to provide a definitive answer yet (Alroy, 2008, Melott, 2008, Melott & Bambach, 2011).

At the present time, therefore, biodiversity cycles cannot currently be completely ruled out empirically, and the possibility of periodicity in the fossil record has some interesting implications for the causes of mass extinction events, which are certainly worth exploring. In this paper, a new conceptual model has been used to demonstrate that a periodic biosphere disturbance need not necessarily be strong enough to cause mass extinctions in itself, but probably acts in conjunction with other, randomly occurring biosphere impacts to cause the major extinction events in the history of life on Earth.

This simple model represents an improvement in various ways: First, the weakness of the periodic disturbance naturally explains why the evidence for cycles in the fossil record is at the limit of statistical credibility. Furthermore, due to the randomness of the non-periodic causes, mass extinctions will occur *around* the peaks of the periodic disturbance (but not exactly at the maxima), so the resulting time series of extinctions is not strictly periodic, in accordance with the data.

Secondly, it could explain the difficulty to find a periodic disturbance strong enough to cause the major extinctions in the fossil record. If a weak periodic cause, together with random perturbations, is sufficient to produce periodic extinctions, there are many more possibilities for cyclic disturbances maybe only slightly enhancing the extinction rate.

Thirdly, it helps to reconcile hypotheses for periodic biodiversity stressors with more traditional explanations for extinction events such as astronomical impacts or large-scale volcanism, since a combination of periodic and random causes is required to produce true mass extinctions. This also helps to bridge the gap between research on possible periodic impacts on the biosphere and established paleontological wisdom.

Finally, a combined model of periodic and random extinction causes allows to quantify the relative importance of various extinction drivers, at least in principle. Although current data-sets and our incomplete understanding of extinction mechanisms restrict our ability to place strong limits on periodic extinction causes, the preliminary analysis in this paper suggests that their contribution to the major extinction epochs in Earth's history is probably comparatively small.

A   Description of the data-sets used in the model tests

De-trended extinction-rate data for marine invertebrate genera were taken from the Paleobiology Database (http://www.paleodb.org, Alroy *et al.* 2008); these are the data shown in Figure 2 of Alroy (2008). Since the primary focus

of the model is a description of the major extinction events and not in the general trend in extinction rate (a secular decline over the Phanerozoic) the de-trended time series for the extinction rate is used for the analysis.

Volcanic perturbations $V(\tau)$ during the Phanerozoic are taken from a compilation of large igneous provinces (Ernst & Buchan 2001, updated and available online at http://www.largeigneousprovinces.org/, accessed 23 September 2009). Although the volume of the magma is probably the best indicator of the impact of a volcanic event, it is generally poorly determined due to erosion. Here the area of the province is used as a proxy for $V(\tau)$. Following Arens & West (2008) the sample is restricted to continental provinces with reasonable information on the age of the eruption, leaving 19 large igneous provinces. For longer eruption periods the signal is distributed equally over the entire age interval.

Data on impact structures were obtained from the Earth Impact Database (http://www.unb.ca/passc/ImpactDatabase/, accessed 23 September 2009) which currently contains 176 confirmed impact craters. The environmental effects of impacts are assumed to depend on the energy Y of the impact, which is computed from the diameter D of the crater (measured in kilometres) according to $Y = 34\,\mathrm{PJ}\,D^{3.4}$ (Toon *et al.*, 1997). The analysis was restricted to impacts during the Phanerozoic and to impact diameters larger than 10 kilometres, resulting in 43 impact structures used in the analysis. Age errors were taken into account by distributing the signal equally over all sub-stages within the error interval. For both volcanic eruptions and impacts the age scale is adjusted to match the one for the extinction curve.

B   Description of the model for the extinction rate

In the model, the de-trended extinction rate is described using a simple linear model, in which the total extinction rate is the sum of the background extinction rate E_b, a periodic contribution E_p, a contribution from flood-basalt volcanism E_v and one from bolide impacts E_i:

$$E(\tau) \;=\; E_\mathrm{b}(\tau) + E_\mathrm{p}(\tau) + E_\mathrm{v}(\tau) + E_\mathrm{i}(\tau). \tag{4}$$

Since the extinction rate is already de-trended, the background extinction

rate E_b is described by a constant a_b:

$$E_\mathrm{b}\left(\tau\right) \; = \; a_\mathrm{b}. \tag{5}$$

The periodic signal is parametrised by a sine wave with amplitude a_p, period T and phase φ:

$$E_\mathrm{p}\left(\tau\right) \; = \; a_\mathrm{p}\left[1 \, + \, \sin\left(\frac{2\pi}{T} + \varphi\right)\right]. \tag{6}$$

For simplicity (and lack of detailed knowledge), linear scaling relations are assumed for the biological effects of large-scale volcanic eruptions $V(\tau)$ and bolide impacts $I(\tau)$:

$$
\begin{aligned}
E_\mathrm{v}\left(\tau\right) &\;=\; a_\mathrm{v}\, V(\tau) \text{ and} & (7)\\
E_\mathrm{i}\left(\tau\right) &\;=\; a_\mathrm{i}\, I(\tau), & (8)
\end{aligned}
$$

where $V(\tau)$ and $I(\tau)$ are estimates of the perturbations caused by flood-basalt volcanism and bolide impacts in the geological past, yielding the full model for the extinction rate E as a function of age τ

$$E\left(\tau\right) \; = \; a_\mathrm{b} + a_\mathrm{p}\left[1 \, + \, \sin\left(\frac{2\pi}{T} + \varphi\right)\right] + a_\mathrm{v}\, V(\tau) + a_\mathrm{i}\, I(\tau) \tag{9}$$

given in Equation (3) in the main text of the paper.

References

Alroy, J. 2008: *Dynamics of origination and extinction in the marine fossil record*, Proceedings of the National Academy of Sciences, 105, 11536

Alroy, J., Aberhan, M., Bottjer, D. J., Foote, M., Fursich, F. T., Harries, P. J., Hendy, A. J. W., Holland, S. M., *et al.* 2008: *Phanerozoic Trends in the Global Diversity of Marine Invertebrates*, Science, 321, 97

Arens, N. C. & West, I. D. 2008: *Press-pulse: a general theory of mass extinction?*, Paleobiology, 34, 456

Bailer-Jones, C. A. L. 2009: *The evidence for and against astronomical impacts on climate change and mass extinctions: A review*, International Journal of Astrobiology, 8, 213

Bambach, R. K. 2006: *Phanerozoic biodiversity mass extinctions*, Annual Review of Earth and Planetary Sciences, 34, 127

Benzi, R., Parisi, G., Sutera, A., & Vulpiani, A. 1982: *Stochastic resonance in climatic change*, Tellus, 34, 10

Burnham, K. P. & Anderson, D. R. 2002: *Model selection and multimodel inference: a practical information-theoretic approach*, Springer, New York

Chapman, C. R. 2004: *The hazard of near-Earth asteroid impacts on earth*, Earth and Planetary Science Letters, 222, 1

Cornette, J. L. 2007: *Gauss-Vaníček and Fourier Transform Spectral Analyses of Marine Diversity*, Computing in Science and Engineering, 9, 61

Crowley, T. J. & North, G. R. 1988: *Abrupt Climate Change and Extinction Events in Earth History*, Science, 240, 996

Davis, M., Hut, P., & Muller, R. A. 1984: *Extinction of species by periodic comet showers*, Nature, 308, 715

Ellis, J. & Schramm, D. N. 1995: *Could a nearby supernova explosion have caused a mass extinction?*, Proceedings of the National Academy of Sciences of the United States of America, 92, 235

Ernst, R. E. & Buchan, K. L. 2001: *Large mafic magmatic events through time and links to mantle plume-heads*, in: Mantle Plumes: Their Identification Through Time. Geological Society of America Special Paper 352, ed. R. E. Ernst & K. L. Buchan, Geological Society of America, Boulder, Colorado, 483

Feulner, G. 2009: *Climate-Modelling of Mass-Extinction Events: a Review*, International Journal of Astrobiology, 8, 207

Ganopolski, A. & Rahmstorf, S. 2002: *Abrupt Glacial Climate Changes due to Stochastic Resonance*, Physical Review Letters, 88, 038501

Hallam, A. 1984: *Pre-Quaternary Sea-Level Changes*, Annual Review of Earth and Planetary Sciences, 12, 205

Hallam, A. & Wignall, P. B. 1999: *Mass extinctions and sea-level changes*, Earth-Science Reviews, 48, 217

Heisler, J., Tremaine, S., & Alcock, C. 1987: *The frequency and intensity of comet showers from the Oort cloud*, Icarus, 70, 269

Holling, C. S. 1973: *Resilience and Stability of Ecological Systems*, Annual Review of Ecology and Systematics, 4, 1

Kaib, N. A. & Quinn, T. 2009: *Reassessing the Source of Long-Period Comets*, Science, 325, 1234

Lieberman, B. S. & Melott, A. L. 2007: *Considering the Case for Biodiversity Cycles: Re-Examining the Evidence for Periodicity in the Fossil Record*, PLoS ONE, 2, e759

Martin, O., Cardenas, R., Guimarais, M., Peñate, L., Horvath, J., & Galante, D. 2010: *Effects of gamma ray bursts in Earth's biosphere*, Astrophysics and Space Science, 326, 61

May, R. M. 1977: *Thresholds and breakpoints in ecosystems with a multiplicity of stable states*, Nature, 269, 471

Medvedev, M. V. & Melott, A. L. 2007: *Do Extragalactic Cosmic Rays Induce Cycles in Fossil Diversity?*, The Astrophysical Journal, 664, 879

Melott, A. L. 2008: *Long-Term Cycles in the History of Life: Periodic Biodiversity in the Paleobiology Database*, PLoS ONE, 3, e4044

Melott, A. L. & Bambach, R. K. 2010: *Nemesis reconsidered*, Monthly Notices of the Royal Astronomical Society, 407, L99

Melott, A. L. & Bambach, R. K. 2011: *A ubiquitous ∼62-Myr periodic fluctuation superimposed on general trends in fossil biodiversity. I. Documentation*, Paleobiology, 37, 92, preprint arXiv:1005.4393

Melott, A. L. & Thomas, B. C. 2009: *Late Ordovician geographic patterns of extinction compared with simulations of astrophysical ionizing radiation damage*, Paleobiology, 35, 311

Napier, W. M. & Clube, S. V. M. 1979: *A theory of terrestrial catastrophism*, Nature, 282, 455

Omerbashich, M. 2006: *Gauss-Vaníček Spectral Analysis of the Sepkoski Compendium: No New Life Cycles*, Computing in Science and Engineering, 8, 26

Overholt, A. C., Melott, A. L., & Pohl, M. 2009: *Testing the Link Between Terrestrial Climate Change and Galactic Spiral Arm Transit*, Astrophysical Journal Letters, 705, L101

Peters, S. E. 2008: *Environmental determinants of extinction selectivity in the fossil record*, Nature, 454, 626

Peters, S. E. & Foote, M. 2002: *Determinants of extinction in the fossil record*, Nature, 416, 420

Prokoph, A., Ernst, R. E., & Buchan, K. L. 2004: *Time-Series Analysis of Large Igneous Provinces: 3500 Ma to Present*, Journal of Geology, 112, 1

Rampino, M. R. & Stothers, R. B. 1984: *Terrestrial mass extinctions, cometary impacts and the sun's motion perpendicular to the galactic plane*, Nature, 308, 709

Raup, D. M. & Sepkoski, J. J. 1982: *Mass Extinctions in the Marine Fossil Record*, Science, 215, 1501

Raup, D. M. & Sepkoski, J. J. 1984: *Periodicity of Extinctions in the Geologic Past*, Proceedings of the National Academy of Sciences of the United States of America-Biological Sciences, 81, 801

Rohde, R. A. & Muller, R. A. 2005: *Cycles in fossil diversity*, Nature, 434, 208

Schaeffer, N. & Manga, M. 2001: *Interaction of rising and sinking mantle plumes*, Geophysical Research Letters, 28, 455

Scheffer, M., Carpenter, S., Foley, J. A., Folke, C., & Walker, B. 2001: *Catastrophic shifts in ecosystems*, Nature, 413, 591

Smith, A. B. & McGowan, A. J. 2005: *Cyclicity in the fossil record mirrors rock outcrop area*, Biology Letters, 1, 443

Toon, O. B., Zahnle, K., Morrison, D., Turco, R. P., & Covey, C. 1997: *Environmental Perturbations Caused by the Impacts of Asteroids and Comets*, Rev. Geophys., 35, 41

van Nes, E. H. & Scheffer, M. 2004: *Large Species Shifts Triggered by Small Forces*, The American Naturalist, 164, 255

White, R. & Saunders, A. 2005: *Volcanism, impact and mass extinctions: incredible or credible coincidences?*, Lithos, 79, 299

Whitmire, D. P. & Jackson, A. A. 1984: *Are periodic mass extinctions driven by a distant solar companion?*, Nature, 308, 713

Wignall, P. 2004: *Causes of mass extinctions*, in: Extinctions in the History of Life, ed. P. Taylor, Cambridge University Press, 119–150

Wignall, P. 2005: *Volcanism and mass extinctions*, in: Volcanoes and the Environment, ed. J. Martí & G. Ernst, Cambridge University Press, pp. 207–226

Wignall, P. B. & Twitchett, R. J. 1996: *Oceanic Anoxia and the End Permian Mass Extinction*, Science, 272, 1155
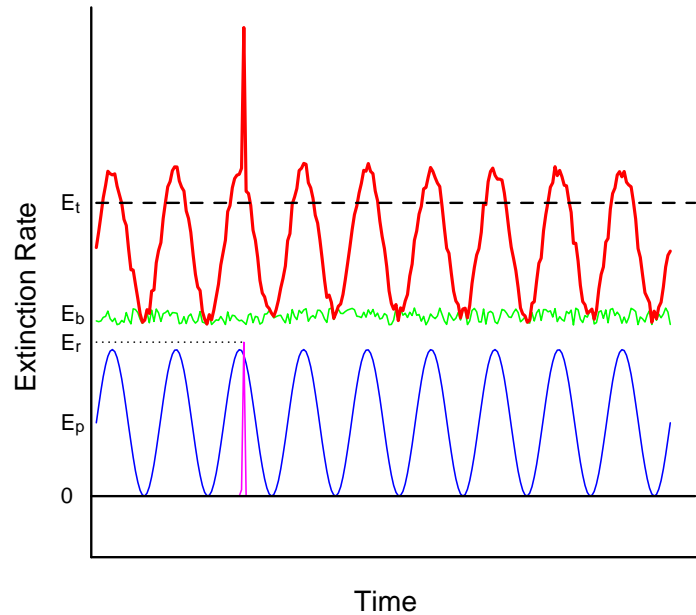
Figure 1: Illustration of the conceptual model. The Figure shows the extinction rate as a function of time. The total extinction rate (*red*) is a combination of the background extinction rate (*green*, E_b), one random event with strongly elevated extinction rate E_r (*magenta*) and a periodic perturbation (*blue*) with amplitude E_p. The threshold extinction rate E_t above which the extinction forcings would be defined as mass extinction is shown as a dashed line. In this case of a strong periodic extinction driver one would find a major extinction event whenever the periodic signal peaks, and particularly severe extinctions when a peak coincides with a random event.
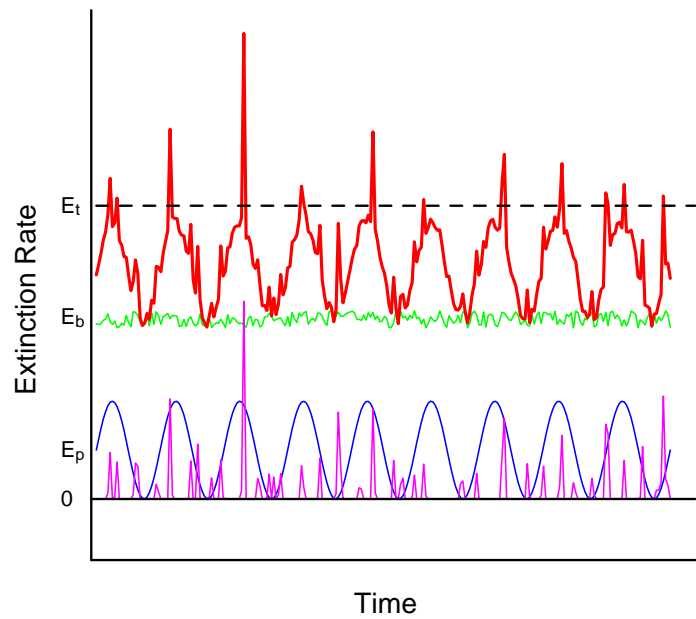
Figure 2: Same as Figure 1, but for a periodic extinction signal too weak to cause a major extinction in itself. In this case of a comparatively weak periodic extinction signal, frequent random events push the total extinction rate above the threshold of a true mass extinction.
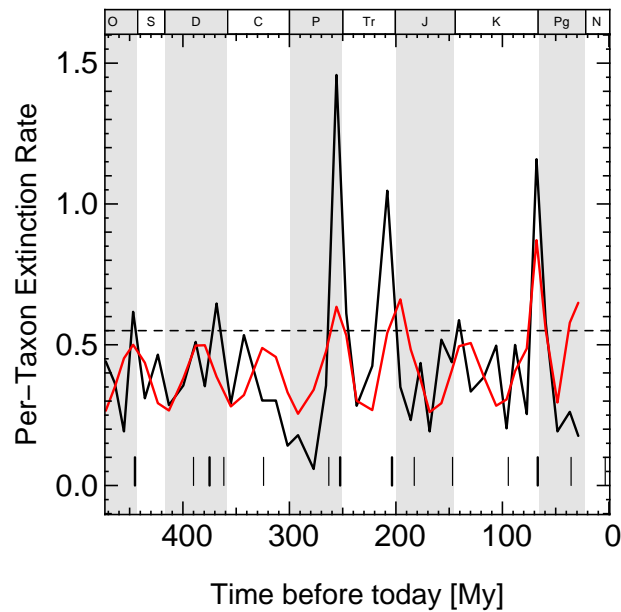
Figure 3: De-trended per-taxon extinction rates of marine invertebrate genera from Alroy (2008) as a function of time (*black*) and the results of the model fit (*red*). The *dashed line* shows an estimate for the threshold for a mass extinction event chosen to select the 'big five'. The dates for the 18 mass extinction events during the Phanerozoic (Bambach, 2006) are indicated at the bottom, with the 'big five' marked by thick lines. O: Ordovician, S: Silurian, D: Devonian, C: Carboniferous, P: Permian, Tr: Triassic, J: Jurassic, K: Cretaceous, Pg: Paleogene, N: Neogene.

Table 1: Results of the fit to the data for the model with and without the periodic extinction component. Model parameters are the background extinction rate a_b, the amplitude a_p, period T and phase φ of a periodic perturbation, and coefficients a_v and a_i translating the area of large igneous provinces and the energy of bolide impacts into extinction rate. Both χ^2 for the fit and the weights w from Akaike's Information Criterion are given in the last two columns.

Model	a_b	a_p	T [Myr]	φ [rad]	a_v [$10^{-6}\,\mathrm{km}^{-2}$]	a_i [$10^{-24}\,\mathrm{J}^{-1}$]	χ^2	w
Periodic	0.25 ± 0.08	0.13 ± 0.05	63.5 ± 3.0	1.0 ± 0.9	0.15 ± 0.12	0.13 ± 0.08	126.23	0.9955
Random	0.37 ± 0.03				0.17 ± 0.06	0.12 ± 0.05	144.78	0.0045